

Problemas de Calentamiento I.

1. $y(x, t) = (6.50 \text{ mm}) \cos 2\pi \left(\frac{x}{28.0 \text{ cm}} - \frac{t}{0.0360 \text{ s}} \right)$

Recuerda que $y(x, t) = A \cos(kx - \omega t)$ donde

$$k = \frac{2\pi}{\lambda} \quad y \quad \omega = \frac{2\pi}{T}$$

Por lo tanto $\lambda = 28 \text{ cm}$ y $T = 0.0360 \text{ s}$

$A = 6.50 \text{ mm}$

a) 6.50 mm

b) 28 cm

c) $k = \frac{1}{T} = \frac{1}{0.0360 \text{ s}}$

d) $v = \lambda f = (28 \times 10^{-2} \text{ m}) \left(\frac{1}{0.0360 \text{ s}} \right)$

e) $+x$; una onda en dirección $-x$

Escriba una función $y(x, t) = A \cos(kx + \omega t)$.

~~i De qué otra forma~~

$$2. \quad v = 344 \text{ m/s}$$

$$a) \quad \lambda = ? \quad f = 784 \text{ Hz} = 784 \text{ s}^{-1}$$

Recuerda que $v = \lambda f \Rightarrow \lambda = \frac{v}{f} = \frac{344 \text{ m/s}}{784 \text{ s}^{-1}}$

$$3. \quad \lambda_1 = 400 \text{ nm} = 400 \times 10^{-9} \text{ m}$$

$$\lambda_2 = 700 \text{ nm} = 700 \times 10^{-9} \text{ m}$$

$$v = 3 \times 10^8 \text{ m/s}$$

Límites de frecuencia: $v = \lambda f \Rightarrow f = \frac{v}{\lambda}$

$$f_1 = \frac{v}{\lambda_2} = \frac{3 \times 10^8 \text{ m/s}}{700 \times 10^{-9} \text{ m}}$$

$$f_2 = \frac{v}{\lambda_1} = \frac{3 \times 10^8 \text{ m/s}}{400 \times 10^{-9} \text{ m}}$$

y periodo $T_1 = \frac{1}{f_2} = \frac{400 \times 10^{-9} \text{ m}}{3 \times 10^8 \text{ m/s}}$

$$T_2 = \frac{1}{f_1} = \frac{700 \times 10^{-9} \text{ m}}{3 \times 10^8 \text{ m/s}}$$

$$4 \text{ a) } y(x, t) = A \cos 2\pi f \left(\frac{x}{v} - t \right)$$

$$= A \cos 2\pi f \cdot \frac{1}{v} (x - vt) \quad (v = \lambda f)$$

$$= A \cos \frac{2\pi}{\lambda} (x - vt) \quad \checkmark$$

$$b) \quad v_y = \frac{\partial y(x, t)}{\partial t} = -A \cdot (2\pi f) (-1) \sin \left[2\pi f \frac{x}{v} - t \right]$$

$$0' \quad v_y = -A \frac{2\pi}{\lambda} (-v) \sin \left[\frac{2\pi}{\lambda} (x - vt) \right]$$

$$= A \left(\frac{2\pi v}{\lambda} \right) \sin \left[\frac{2\pi}{\lambda} (x - vt) \right]$$